

1. Particles P and Q move in a plane with constant velocities. At time $t = 0$ the position vectors of P and Q , relative to a fixed point O in the plane, are $(16\mathbf{i} - 12\mathbf{j})$ m and $(-5\mathbf{i} + 4\mathbf{j})$ m respectively. The velocity of P is $(\mathbf{i} + 2\mathbf{j})$ m s⁻¹ and the velocity of Q is $(2\mathbf{i} + \mathbf{j})$ m s⁻¹

Find the shortest distance between P and Q in the subsequent motion.

(7)



3.

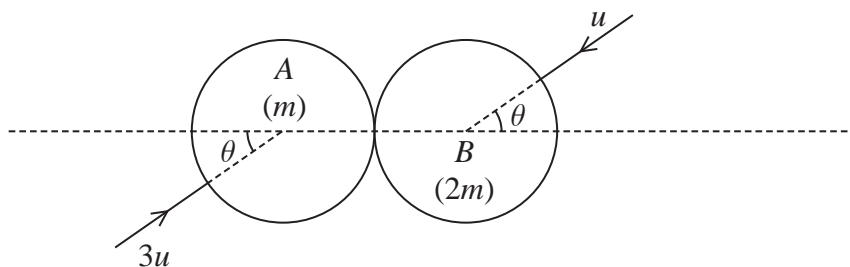


Figure 1

Two smooth uniform spheres *A* and *B* with equal radii have masses m and $2m$ respectively. The spheres are moving in opposite directions on a smooth horizontal surface and collide obliquely. Immediately before the collision, *A* has speed $3u$ with its direction of motion at an angle θ to the line of centres, and *B* has speed u with its direction of motion at an angle θ to the line of centres, as shown in Figure 1. The coefficient of restitution between the spheres is $\frac{1}{8}$

Immediately after the collision, the speed of *A* is twice the speed of *B*.

Find the size of the angle θ .

(12)



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Question 4 continued

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Q4

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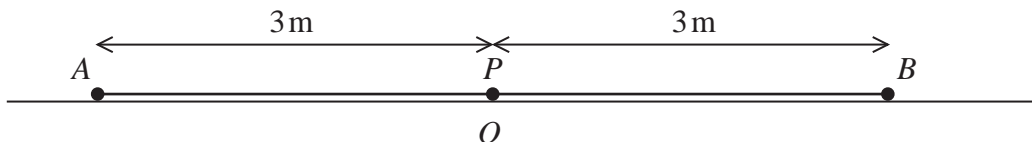


Figure 2

A particle P of mass 1.5 kg is attached to the midpoint of a light elastic spring AB , of natural length 2 m and modulus of elasticity 12 N. The end A of the spring is attached to a fixed point on a smooth horizontal floor. The end B is held at a point on the floor where $AB = 6$ m.

At time $t = 0$, P is at rest on the floor at the point O , where $AO = 3$ m, as shown in Figure 2. The end B is now moved along the floor in such a way that AOB remains a straight line and at time t seconds, $t \geq 0$,

$$AB = \left(6 + \frac{1}{4} \sin 2t \right) \text{ m}$$

At time t seconds, $AP = (3 + x)$ m.

(a) Show that, for $t \geq 0$,

$$\frac{d^2x}{dt^2} + 16x = 2 \sin 2t \tag{5}$$

The general solution of this differential equation is

$$x = C \cos 4t + D \sin 4t + \frac{1}{6} \sin 2t$$

where C and D are constants.

(b) Find the time at which P first comes to instantaneous rest. (5)



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Question 5 continued

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Q5

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P 4 4 8 4 0 A 0 1 9 2 8

6.

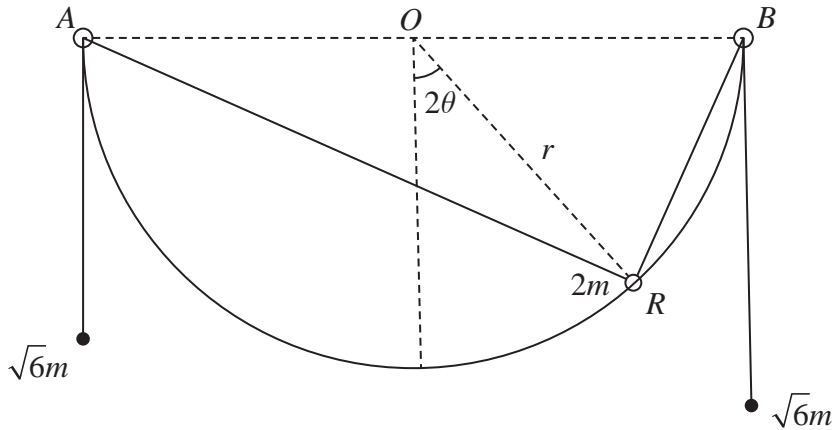


Figure 3

A smooth wire, with ends A and B , is in the shape of a semicircle of radius r . The line AB is horizontal and the midpoint of AB is O . The wire is fixed in a vertical plane. A small ring R of mass $2m$ is threaded on the wire and is attached to two light inextensible strings. One string passes through a small smooth ring fixed at A and is attached to a particle of mass $\sqrt{6}m$. The other string passes through a small smooth ring fixed at B and is attached to a second particle of mass $\sqrt{6}m$. The particles hang freely under gravity, as shown in Figure 3. The angle between the radius OR and the downward vertical is 2θ , where $-\frac{\pi}{4} < \theta < \frac{\pi}{4}$

(a) Show that the potential energy of the system is

$$2mgr(2\sqrt{3}\cos\theta - \cos 2\theta) + \text{constant} \tag{6}$$

(b) Find the values of θ for which the system is in equilibrium. (4)

(c) Determine the stability of the position of equilibrium for which $\theta > 0$ (3)



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Question 6 continued

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Q6

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(Total 13 marks)



7.

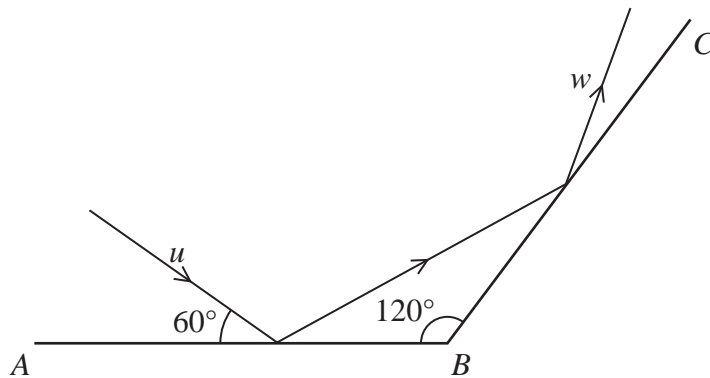


Figure 4

Figure 4 represents the plan view of part of a smooth horizontal floor, where AB and BC are smooth vertical walls. The angle between AB and BC is 120° . A ball is projected along the floor towards AB with speed $u \text{ m s}^{-1}$ on a path at an angle of 60° to AB . The ball hits AB and then hits BC . The ball is modelled as a particle. The coefficient of restitution between the ball and each wall is $\frac{1}{2}$

(a) Show that the speed of the ball immediately after it has hit AB is $\frac{\sqrt{7}}{4}u$. (6)

The speed of the ball immediately after it has hit BC is $w \text{ m s}^{-1}$

(b) Find w in terms of u . (7)



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Question 7 continued

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(Total 13 marks)

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Q7

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